

Pondération dynamique dans un cadre multi-tâche pour réseaux de neurones profonds

RFIA 2016



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INSA

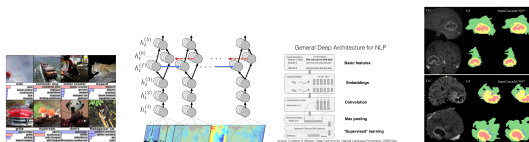
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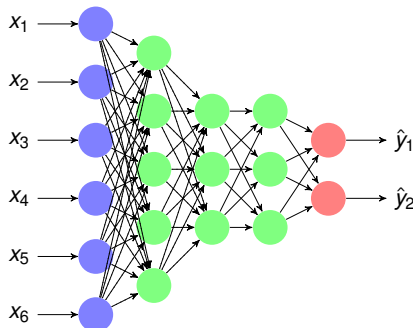
29 June, 2016



- Large data
- Calculation power (GPUS, clouds)

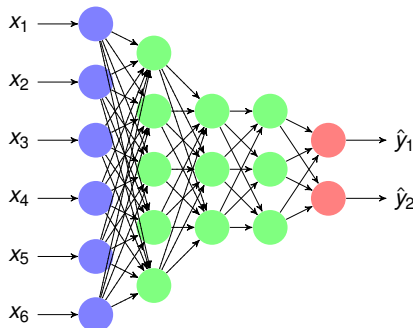
- Dropout
- Momentum, AdaDelta, AdaGrad, RMSProp, Adam, Adamax
- Maxout, Local response normalization, local contrast normalization, batch normalization
- RELU
- Torch, Caffe, Pylearn2, Theano, TensorFlow
- CNN, RBM, RNN

Deep neural networks (DNN)



- Feed-forward neural network
- Back-propagation error
- Training **deep** neural networks is **difficult**
 - ⇒ **Vanishing gradient**
 - ⇒ **Pre-training technique** [Y.Bengio et al. 06, G.E.Hinton et al. 06]
 - ⇒ **More parameters** ⇒ **Need more data**
 - ⇒ **Use unlabeled data**

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Semi-supervised learning

General case:

$$Data = \{ \underbrace{\text{labeled data } (\mathbf{x}, \mathbf{y})}_{\text{expensive (money, time), few}}, \underbrace{\text{unlabeled data } (\mathbf{x}, --)}_{\text{cheap, abundant}} \}$$

E.g:

- Collect images from the internet
- Medical images

⇒ semi-supervised learning:

Exploit unlabeled data to improve the **generalization**

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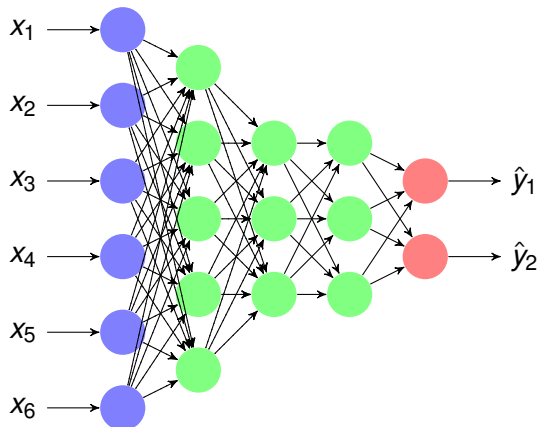
Pre-training and semi-supervised learning

The pre-training technique can exploit the unlabeled data

A **sequential** transfer learning performed in 2 steps:

- 1 **Unsupervised task** (\mathbf{x} labeled and unlabeled data)
- 2 **Supervised task** ((\mathbf{x}, \mathbf{y}) labeled data)

Layer-wise pre-training: auto-encoders

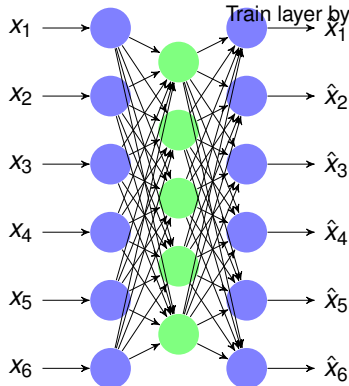


A DNN to train

Layer-wise pre-training: auto-encoders

1) Step 1: Unsupervised layer-wise pre-training

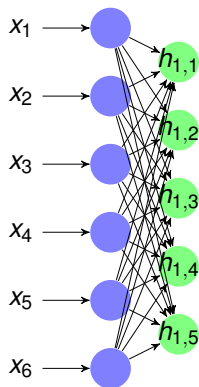
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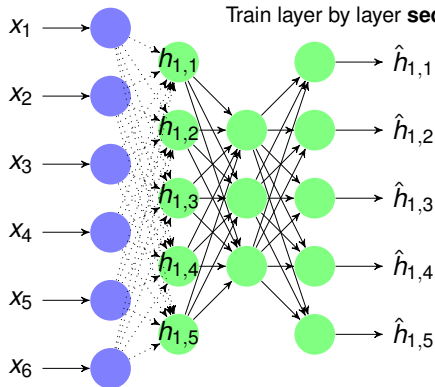
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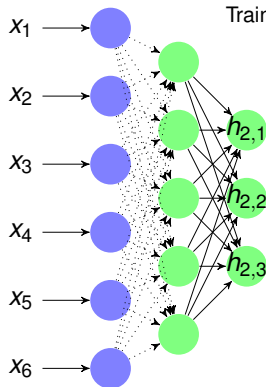
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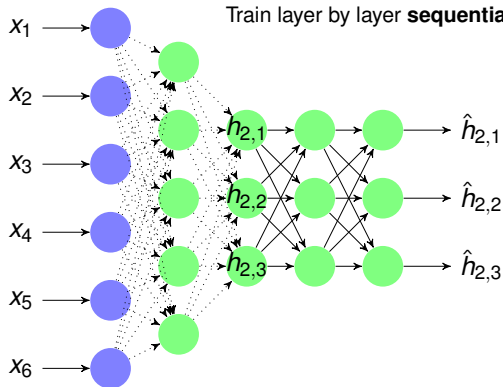
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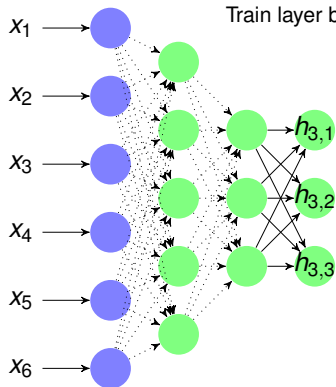
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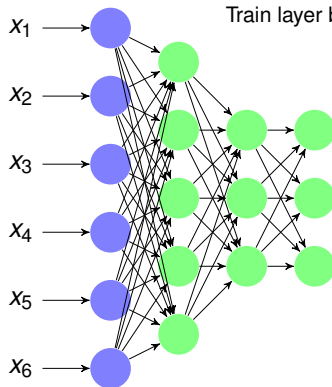
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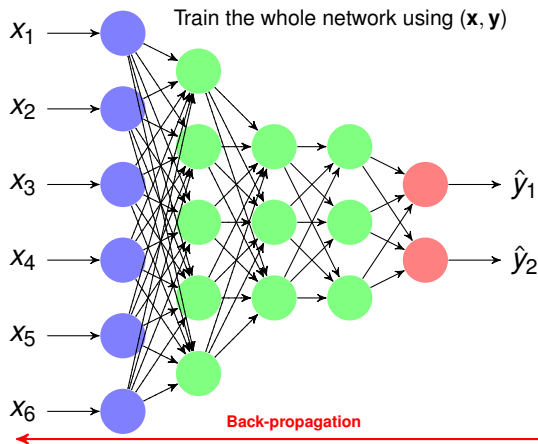


At each layer:

- ⇒ What hyper-parameters to use? When to stop training?
- ⇒ How to make sure that the pre-training improves the supervised task?

Layer-wise pre-training: auto-encoders

2) Step 2: Supervised training



Pre-training technique: Pros and cons

Pros

- Improve generalization
 - Can exploit unlabeled data
 - Provide better initialization than random
 - Train deep networks
- ⇒ Circumvent the vanishing gradient problem

Cons

- Add more hyper-parameters
 - No good stopping criterion during pre-training phase
- Good criterion for the unsupervised task
But
May not be good for the supervised task

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Proposed solution

Why is it difficult in practice?

⇒ **Sequential** transfer learning

Possible solution:

⇒ **Parallel** transfer learning

Why in parallel?

- Interaction between tasks
- Reduce the number of hyper-parameters to tune
- Provide **one stopping criterion**

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Parallel transfer learning: Tasks combination

$$\text{Train cost} = \text{supervised task} + \underbrace{\text{unsupervised task}}_{\text{reconstruction}}$$

l labeled samples, *u* unlabeled samples, \mathbf{w}_{sh} : shared parameters.

Reconstruction (auto-encoder) task:

$$\mathcal{J}_r(\mathcal{D}; \mathbf{w}' = \{\mathbf{w}_{sh}, \mathbf{w}_r\}) = \sum_{i=1}^{l+u} C_r(\mathcal{R}(\mathbf{x}_i; \mathbf{w}'), \mathbf{x}_i) .$$

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Problem

How to **fix** λ_s, λ_r ?

Intuition

At the end of the training, only \mathcal{J}_s should matters

Tasks combination with evolving weights (our contribution)

$$\mathcal{J}(\mathcal{D}; \{\mathbf{w}_{sh}, \mathbf{w}_s, \mathbf{w}_r\}) = \lambda_s(t) \cdot \mathcal{J}_s(\mathcal{D}; \{\mathbf{w}_{sh}, \mathbf{w}_s\}) + \lambda_r(t) \cdot \mathcal{J}_r(\mathcal{D}; \{\mathbf{w}_{sh}, \mathbf{w}_r\}) .$$

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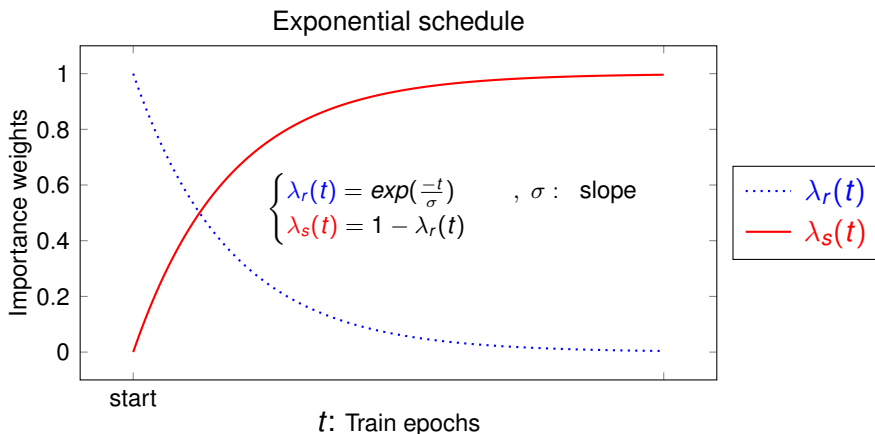
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Tasks combination with evolving weights: Optimization

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Algorithm 1 Training our model for one epoch

- 1: \mathcal{D} is the *shuffled* training set. B a mini-batch.
 - 2: **for** B in \mathcal{D} **do**
 - 3: Make a gradient step toward \mathcal{J}_r using B (update \mathbf{w}')
 - 4: $B_s \leftarrow$ labeled examples of B ,
 - 5: Make a gradient step toward \mathcal{J}_s using B_s (update \mathbf{w})
 - 6: **end for**
-

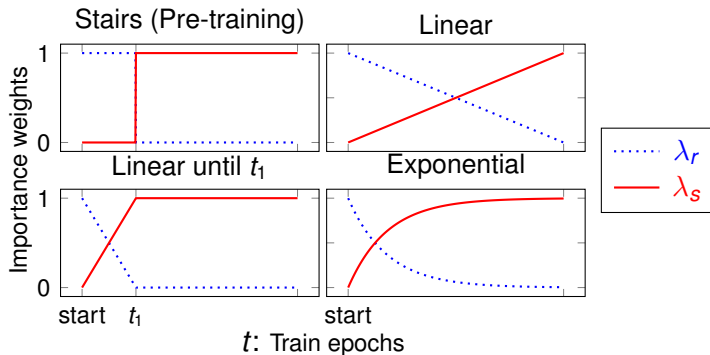
[R.Caruana 97, J.Weston 08, R.Collobert 08, Z.Zhang 15]

Experimental protocol

Objective: Compare Training DNN using different approaches:

- No pre-training (base-line)
- With pre-training (Stairs schedule)
- Parallel transfer learning (proposed approach)

Studied evolving weights schedules:

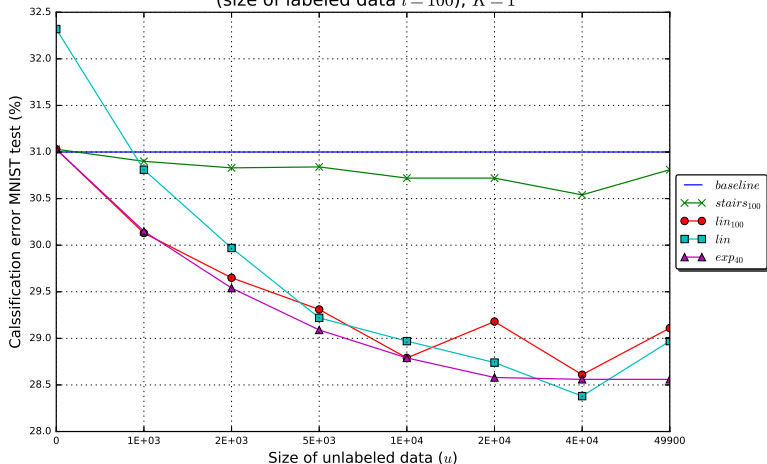


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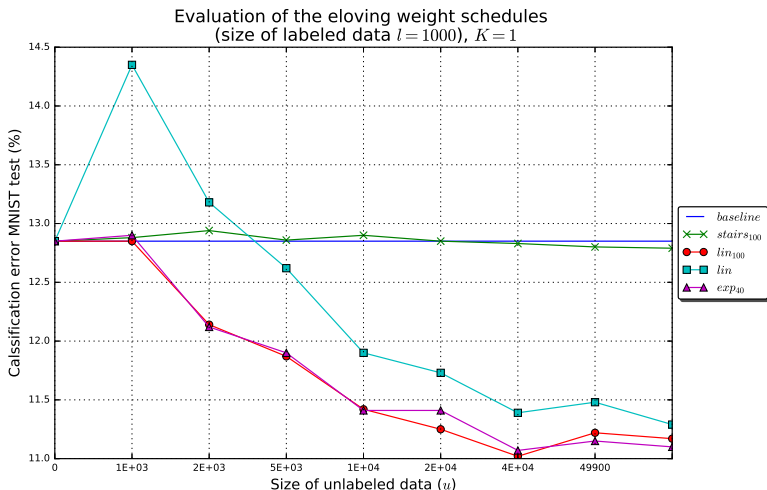
- **Task:** Classification (MNIST)
- **Number of hidden layers K :** 1, 2, 3, 4.
- **Optimization:**
 - **Epochs:** 5000
 - **Batch size:** 600
 - **Options:** No regularization, No adaptive learning rate
- **Hyper-parameters of the evolving schedules:**
 - t_1 : 100 • σ : 40

Shallow networks: ($K = 1$, $l = 1E2$)

Evaluation of the evolving weight schedules
(size of labeled data $l = 100$), $K = 1$

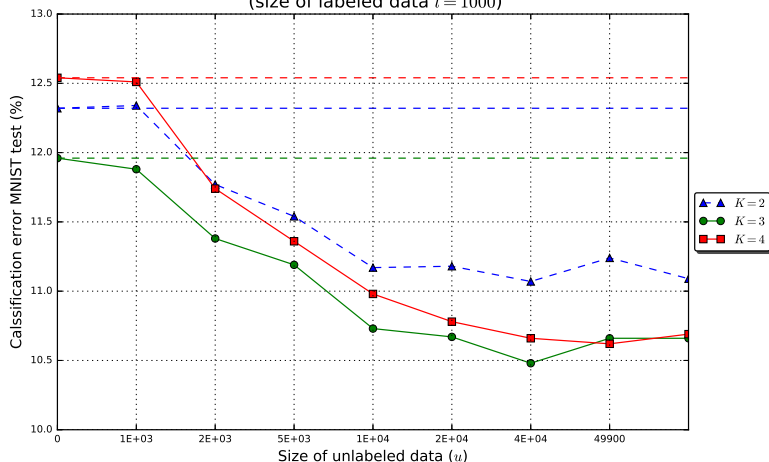


Shallow networks: ($K = 1$, $l = 1E3$)



Deep networks: exponential schedule ($l = 1E3$)

Evaluation of the exp_{40} evolving weight schedule
(size of labeled data $l = 1000$)



Conclusion

- An alternative method to the pre-training.
Parallel transfer learning with evolving weights
- Improve generalization easily.
- Reduce the number of hyper-parameters (t_1 , σ)

Perspectives

- Evolve the importance weight according to the train/validation error.
- Explore other evolving schedules (toward automatic schedule)
- Optimization
- **Extension to structured output problems**

Train cost = **supervised task**
+ **Input unsupervised task**
+ **Output unsupervised task**



Questions

Thank you for your attention,

Questions?